RESISTORS/CAPACITOR CIRCUITS

LAB ELEC 8
REFERENCES: College Board AP
                AP Physics B Exam 2007
                Question 3

INTRODUCTION

The given circuit involves an $\mathcal{E}$ = emf with resistance $R_A = 2R$ in series and also in series two parallel resistances $R_B = 2R$ and $R_C = R$. Note the circuit schematic as shown in Figure 1.

This AP Physics B Exam 2007 question 3, parts (a) and (b) with the switch closed is based on this circuit and involves ranking the current and voltage magnitudes in and across resistance $R_A$, $R_B$, and $R_C$. Included here as page 3 is the list of Electricity and Magnetism equations and symbol definitions, given with the exam.

Values are then given for $\mathcal{E}$ and $R$ to be used in calculating (c), the equivalent circuit resistance, and (d), the current in $R_C$; and also for answering (e).

For (e), the schematic of Figure 1 is changed in removing resistance $R_B$ and replacing it with a capacitor with its capacitance given. Then with the switch closed and steady state currents, the charge on the capacitor is to be calculated.

PURPOSE

To analyze and understand the electrical function and behavior of a direct current (DC) circuit with a power supply and resistors in series and in parallel according to Figure 1. Further, to analyze and understand the resulting behavior when the resistor, $R_B$, in the one parallel branch is replaced by a capacitor.

MATERIALS

<table>
<thead>
<tr>
<th>Battery pack (6 volts)</th>
<th>Capacitor, $\sim 11.5 \times 10^{-6}$F</th>
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</thead>
<tbody>
<tr>
<td>5:220 $\Omega$ resistors</td>
<td>Switch</td>
</tr>
<tr>
<td>8: Clip leads</td>
<td>Multimeter</td>
</tr>
</tbody>
</table>

PRELIMINARY QUESTIONS

1. Compare and explain the total resistance of two “identical” resistors is series and in parallel.
2. Considering the circuit shown in Figure 1 with $R_B$ replaced with a capacitor, give and explain the total resistance of the circuit in terms of $R$ just as the switch is closed.
3. For the resistance/capacitance circuit (of question 2); with the switch closed for “some” time, give and explain the total resistance of the circuit in terms of $R$. 
PROCEDURE/ANALYSIS

The circuit above contains a battery with negligible internal resistance, a closed switch $S$, and three resistors, each with a resistance of $R$ or $2R$.

(a)

i. Rank the currents in the three resistors from greatest to least, with number 1 being the greatest. If two resistors have the same current, give them the same ranking.

_____ $I_A$  _____ $I_B$  _____ $I_C$

ii. Justify your answers.

(b)

i. Rank the voltages across the three resistors from greatest to least, with number 1 being greatest. If two resistors have the same voltage across them, give them the same ranking.

_____ $V_A$  _____ $V_B$  _____ $V_C$

ii. Justify your answers.

For parts (c) through (e), use $\varepsilon = 6V$ and $R = 220 \, \Omega$.

(c) Calculate the equivalent resistance of the circuit.

(d) Calculate the current in resistor $R_C$.

(e) The switch $S$ is opened, resistor $R_B$ is removed and replaced by a capacitor of capacitance $\sim 11.5 \times 10^{-6}$ F, and the switch $S$ is again closed. Calculate the charge on the capacitor after all the currents have reached their final steady-state values.

For parts (a), (b), (c), (d), and (e); use the multimeter taking measurements to check your answers. Record, discuss and compare your results.
Resistors/Capacitor Circuits

ELECTRICITY AND MAGNETISM

\[ F = \frac{1}{4\pi \varepsilon_0} \frac{q_1 q_2}{r^2} \]

\[ \mathbf{E} = \frac{F}{q} \]

\[ U_E = qV = \frac{1}{4\pi \varepsilon_0} \frac{q_1 q_2}{r} \]

\[ E_{\text{avg}} = \frac{V}{d} \]

\[ V = \frac{1}{4\pi \varepsilon_0} \sum_i \frac{q_i}{r_i} \]

\[ C = \frac{Q}{V} \]

\[ C = \frac{\varepsilon_0 A}{d} \]

\[ U_c = \frac{1}{2} QV = \frac{1}{2} CV^2 \]

\[ I_{\text{avg}} = \frac{\Delta Q}{\Delta t} \]

\[ R = \frac{\rho \ell}{A} \]

\[ V = IR \]

\[ P = IV \]

\[ C_p = \sum_i C_i \]

\[ \frac{1}{C_s} = \sum_i \frac{1}{C_i} \]

\[ R_S = \sum_i R_i \]

\[ \frac{1}{R_p} = \sum_i \frac{1}{R_i} \]

\[ F_B = qvB \sin \theta \]

\[ F_B = BIl \sin \theta \]

\[ B = \frac{\mu_0 I}{2\pi r} \]

\[ \phi_m = BA \cos \phi \]

\[ \varepsilon_{\text{avg}} = -\frac{\Delta \phi_m}{\Delta t} \]

\[ \varepsilon = B\ell \nu \]

\[ A = \text{area} \]

\[ B = \text{magnetic field} \]

\[ C = \text{capacitance} \]

\[ d = \text{distance} \]

\[ E = \text{electric field} \]

\[ \varepsilon = \text{emf} \]

\[ F = \text{force} \]

\[ I = \text{current} \]

\[ \ell = \text{length} \]

\[ P = \text{power} \]

\[ Q = \text{charge} \]

\[ q = \text{point charge} \]

\[ R = \text{resistance} \]

\[ r = \text{distance} \]

\[ t = \text{time} \]

\[ U = \text{potential (stored) energy} \]

\[ V = \text{electric potential or potential difference} \]

\[ v = \text{velocity or speed} \]

\[ \rho = \text{resistivity} \]

\[ \theta = \text{angle} \]

\[ \phi_m = \text{magnetic flux} \]