

Pendulum Periods

LAB MECH 16. CALC

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INTRODUCTION

A swinging pendulum keeps a very regular beat. It is so regular, in fact, that for many years the pendulum was the heart of clocks used in astronomical measurements at the Greenwich Observatory.

There are at least three things you could change about a pendulum that might affect the *period* (the time for one complete cycle):

- the amplitude of the pendulum swing
- the length of the pendulum, measured from the center of the pendulum bob to the point of support
- the mass of the pendulum bob

To investigate the pendulum, you need to do a *controlled* experiment; that is, you need to make measurements, changing only one variable at a time. Conducting controlled experiments is a basic principle of scientific investigation.

In this experiment, you will use a Photogate capable of about 4-ms precision to measure the period of one complete swing of a pendulum. By conducting a series of controlled experiments with the pendulum, you can determine how each of these quantities affects the period.

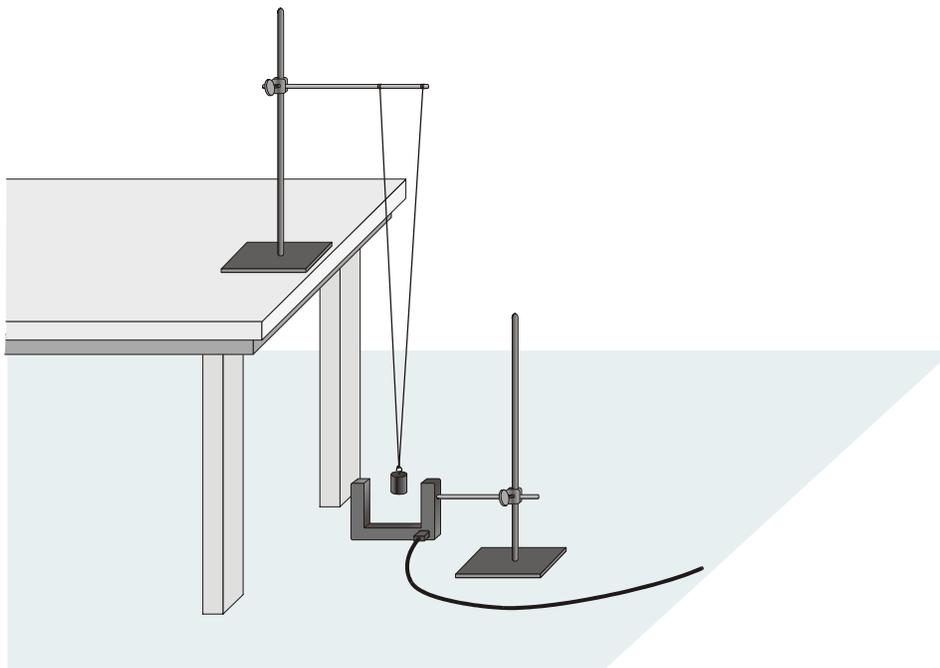


Figure 1

PURPOSE

The purpose of this experiment is to study and measure the period of a pendulum as a function of amplitude, length, and mass of the pendulum bob.

MATERIALS

LabPro or CBL 2 interface	Protractor
TI Graphing Calculator	Masses of 0.100 kg, 0.200 kg, 0.300 kg
DataGate program	Meter stick
Vernier Photogate	Graphical Analysis (optional) or graph paper
Pendulum bob	2 ring stands, pendulum clamp, & angle clamp
Mass hanger	
String	

PRELIMINARY QUESTIONS

1. Make a pendulum by tying a 1.00 m string to a mass. Hold the string in your hand and let the mass swing. Observing only with your eyes, does the period depend on the length of the string? Does the period depend on the amplitude of the swing?
2. Try a different mass on your string. Does the period seem to depend on the mass?

PROCEDURE

1. Use the ring stand to hang the 0.200 kg mass from two strings. Attach the strings to a horizontal rod about 0.10 m apart, as shown in Figure 1. This arrangement will let the mass swing only along a line, and will prevent the mass from striking the Photogate. The length of the pendulum is the distance from the point on the rod halfway between the strings to the center of the mass. The pendulum length should be at least 1 m.
2. Attach the Photogate to the second ring stand. Position it so that the mass blocks the Photogate while hanging straight down.
3. Connect the Photogate to the DIG/SONIC input on the CBL 2 or the DIG/SONIC 1 input of the LabPro. Use the black link cable to connect the interface to the TI Graphing Calculator. Firmly press in the cable ends.
4. Turn on the calculator and start the DATAGATE program. Press to reset the program.
5. Set up the calculator for pendulum timing.
 - a. Select SETUP from the main screen.
 - b. Select PENDULUM from the PHOTOGATE SETUP screen.
6. Temporarily hold the mass out of the center of the Photogate. Observe the reading on the calculator screen; you should see --0--, which indicates that the gate is open. Block the Photogate with your hand; note that the Photogate is shown as blocked (--X--). Remove your hand and the display should change to unblocked.
7. Temporarily hold the mass out of the center of the Photogate. Select START to prepare the Photogate.

8. Now you can perform a trial measurement of the period of your pendulum. Hold the mass from about 10° from vertical and release. (For a pendulum that is 1.00 m long, that corresponds to pulling the bob only about 0.15 m to the side.) After the calculator indicates that five trials have been recorded, press **STO▶** to end data collection. The average period is displayed on the calculator screen.
9. To return to the main screen, press **ENTER**. When you are ready measure another period, select START prepare the Photogate. You will use this method for each period measurement below.

Part I Amplitude

10. Determine how the period depends on amplitude. Measure the period for five different amplitudes. Use a range of amplitudes, from just barely enough to unblock the Photogate, to about 30° . Each time, measure the amplitude using the protractor so that the mass with the string is released at a known angle. Repeat this step for each different amplitude. Record the data in your Data Table.

Part II Length

11. Use the method you learned above to investigate the effect of changing pendulum length on the period. Use the 0.200 kg mass and a consistent amplitude of 10° for each trial. Vary the pendulum length in steps of 0.10 m, from 1.00 m to 0.50 m. If you have room, continue to a longer length (up to 2 m). Repeat Steps 7 and 8 for each length. Record the data in the second Data Table below. Measure the pendulum length from the rod to the *middle* of the mass.

Part III Mass

12. Use the three masses to determine if the period is affected by changing the mass. Measure the period of the pendulum constructed with each mass, taking care to keep the distance from the ring stand rod to the center of the mass the same each time, as well as keeping the amplitude the same. Repeat Steps 7 and 8 for each mass, using an amplitude of about 20° . Record the data in your Data Table.

DATA TABLE

Part I Amplitude

Amplitude (°)	Average period (s)

Part II Length

Length (m)	Average period (s)

Part III Mass

Mass (kg)	Average period (s)

ANALYSIS

1. In measuring the pendulum period, should the interface measure the time between two adjacent blocks of the photogate? Or is some other measurement logic used? Why?
2. Using your calculator, Graphical Analysis, or graph paper, plot a graph of pendulum period T vs. amplitude in degrees. Scale each axis from the origin (0,0). According to your data, does the period depend on amplitude? Explain.
3. Using your calculator, Graphical Analysis, or graph paper, plot a graph of pendulum period T vs. length ℓ . Scale each axis from the origin (0,0). Does the period appear to depend on length?
4. Using your calculator, Graphical Analysis, or graph paper, plot the pendulum period vs. mass. Scale each axis from the origin (0,0). Does the period appear to depend on mass? Do you have enough data to answer this conclusively?
5. To examine more carefully how the period T depends on the pendulum length ℓ , create the following two additional graphs of the same data: T^2 vs. ℓ and T vs. ℓ^2 . Of the three period-length graphs, which is closest to a direct proportion; that is, which plot is most nearly a straight line that goes through the origin?
6. Using Newton's laws, we could show that for a simple pendulum the period T is related to the length ℓ and free-fall acceleration g by

$$T = 2\pi\sqrt{\frac{\ell}{g}}, \text{ or } T^2 = \left(\frac{4\pi^2}{g}\right) \times \ell$$

Does one of your graphs support this relationship? Explain. (Hint: Can the term in parentheses be treated as a constant of proportionality?)

EXTENSIONS

1. From your graph of T^2 vs. ℓ , determine a value for g .
2. Given what you observed in this experiment, write a set of rules for constructing a pendulum clock that is reliable under a variety of temperatures.
3. Try a larger range of amplitudes than you used in Part I. If you did not see a change in period with amplitude before, you should now. Check a college physics textbook for an expression for the period of a pendulum at large amplitudes and compare to your own data.
4. Use an air table and air table puck as your pendulum. Tip the air table to a variety of angles, θ , and determine the relationship between the period and the angle.